

## 1500 Chapter 17 Improper Integrals & 18 Applications

### Directions:

I would recommend that you do the following:

1) Complete all of the preparation a head of time. Get a printout of the test to take with paper and pencil .

3)

### Description:

There are 21 multiple choice questions. You must complete and submit this test in Thinkwell BEFORE the deadline. Be sure to answer ALL questions. I would strongly recommend that you check as many questions as possible.

1) QID: 26136

Evaluate the integral  $\int_0^2 \frac{dx}{\sqrt{2-x}}$ .

- $-2\sqrt{2}$   
  $\sqrt{2}$   
  $-\sqrt{2}$   
  $2\sqrt{2}$

2) QID: 19978

What is the correct way to evaluate the improper integral

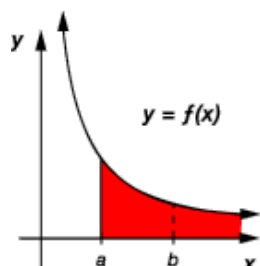
$$\int_{-4}^4 \frac{1}{x^4} dx$$

using subintervals?

- $\int_{-4}^0 \frac{1}{x^4} dx + \int_0^4 \frac{1}{x^4} dx$   
  $\int_{-4}^{-2} \frac{1}{x^4} dx + \int_{-2}^0 \frac{1}{x^4} dx$   
  $\int_0^2 \frac{1}{x^4} dx + \int_2^4 \frac{1}{x^4} dx$   
  $\int_{-4}^{-2} \frac{1}{x^4} dx + \int_{-2}^4 \frac{1}{x^4} dx$

3) QID: 19261

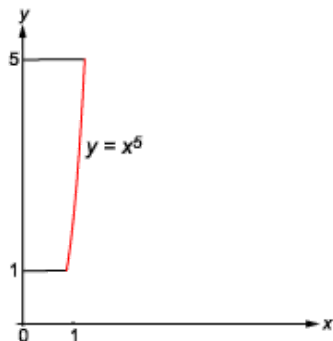
Consider the red region under the curve  $y = f(x)$  where  $x \rightarrow \infty$ . Which of the following expressions correctly describes the limit of the area of the red region?



- $\lim_{x \rightarrow \infty} f(x)$   
  $\int_a^b f(x) dx$   
  $\lim_{b \rightarrow \infty} \int_a^b f(x) dx$   
  $\int_{-\infty}^{\infty} f(x) dx$

4) QID: 18559

Set up the integral that produces the volume of the solid generated by revolving the plane region bounded by  $y = x^5$ ,  $y = 1$ ,  $y = 5$ , and  $x = 0$  about the  $y$ -axis.



- $\int_1^5 y^{2/5} dy$   
  $\int_1^5 \pi y^{1/5} dy$   
  $\int_1^5 \pi y^{10} dy$   
  $\int_1^5 \pi y^{2/5} dy$

5) QID: 18589

Consider the solid of revolution generated by rotating the area bounded by  $y = \sqrt{\cos x}$ , the  $x$ -axis,  $x = 0$  and  $x = \pi/2$  around the  $x$ -axis. What will be the upper limit of integration in the formula to determine the volume using disks?

- 0  
 1  
  $\frac{\pi}{2}$   
  $\pi$

6) QID: 18708

What is the volume of the solid of revolution generated by revolving the area bounded by  $y = 2$ ,  $y = x$ , and  $x = 0$  around the  $x$ -axis?

- $8\pi \text{ units}^3$   
  $\frac{16\pi}{3} \text{ units}^3$   
  $2\pi \text{ units}^3$   
  $\frac{-8\pi}{3} \text{ units}^3$

7) QID: 18714

It takes 10 lb of force to stretch a spring 2 in. What is the stiffness (spring constant) of the spring?

- 5 lb/in  
 5 lb-in  
 5 in/ft  
 5 in/lb

8) QID: 18725

Which of the following is the work done by a constant force  $F$  moving an object along a straight line from  $a$  to  $b$ ?

- $W = F \cdot (a + b)$   
  $W = F \cdot (a - b)$   
  $W = \frac{F}{b - a}$   
  $W = F \cdot (b - a)$

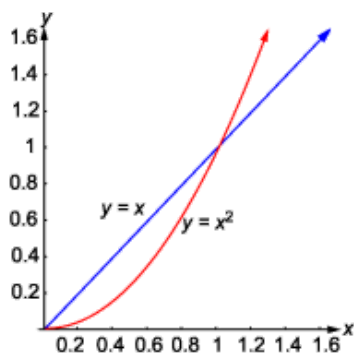
9) QID: 18796

A crane raises a 12,000 N marble sculpture at a constant velocity onto a pedestal 1.5 m above the ground outside an art museum. How much work is done by the crane?

- 180,000 N-m  
 18,000 N-m  
 18,000  
 12,000 N-m

10) QID: 18812

Consider a region bounded by curves  $y = x$  and  $y = x^2$  rotated about the  $x$ -axis. What is the volume of the resulting solid?



- $\frac{\pi}{6}$   
  $\frac{4\pi}{15}$   
  $\frac{2\pi}{15}$   
  $\frac{8\pi}{15}$

11) QID: 20299

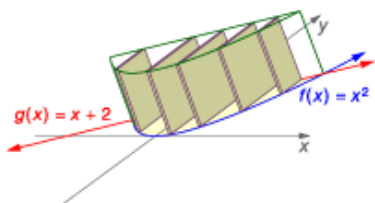
Which of the following is the average value of  $f(x)$  on the interval  $[a, b]$ ?

- $\int_a^b f(x) dx$   
  $\frac{f(b) + f(a)}{b - a}$   
  $\frac{1}{a - b} \int_a^b f(x) dx$   
  $\frac{1}{b - a} \int_a^b f(x) dx$

12) QID: 20988

What is the volume of this solid? The base of the solid is bounded by the curves  $f(x) = x^2$  and  $g(x) = x + 2$ , and the cross-sections perpendicular to the  $x$ -axis are rectangles of height 1.

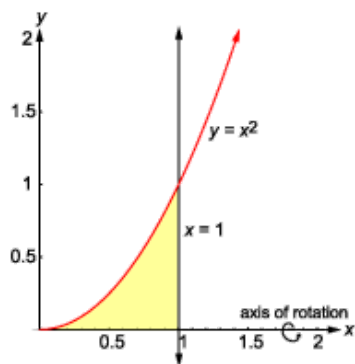
- $3/2$   
  $13/6$   
  $9/2$   
  $7/6$



13) QID: 21445

Which of the following is the volume of the solid of revolution formed by revolving the region bounded by  $y = x^2$  and  $x = 1$  around the  $x$ -axis, where  $x \geq 0$ . Use the cylindrical shell method.

- $\frac{4\pi}{5}$   
  $\frac{\pi}{5}$   
  $\frac{\pi}{2}$   
  $\frac{\pi}{6}$



14) QID: 27330

What is the average value of  $\sin x$  on  $[0, \pi/2]$ ?

- 0  
 1  
  $2/\pi$   
  $1/\pi$

15) QID: 27373

Find the volume of the solid of revolution obtained by rotating the region bounded by  $y = 4 - x^2$ ,  $x = 1$ , the  $x$ -axis, and the  $y$ -axis about the  $y$ -axis.

- $3\pi/2$   
  $7\pi/2$   
  $\pi$   
  $5\pi/2$

16) QID: 27508

What is the volume of the solid of revolution obtained by rotating the region bounded by  $y = 2x^2 + 1$ ,  $x = 1$ , and  $x = 0$  around the  $x$ -axis?

- $\frac{32\pi}{15}$   
  $\frac{47\pi}{5}$   
  $\frac{47\pi}{15}$   
  $\frac{4\pi}{15}$

17) QID: 27638

A force of  $2x + 5$  pounds at a point  $x$  feet from the origin moves an object from  $x = 2$  to  $x = 5$ . What is the work done?

- 25 ft-lb  
 11 ft-lb  
 36 ft-lb  
 46 ft-lb

18) QID: 27735

What is the volume of the solid whose cross-sections perpendicular to the  $x$  axis are squares based on the region bounded by  $y = x$ ,  $y = 0$ , the  $x$ -axis and  $x=1$ ?

- 1  
  $1/3$   
  $1/2$   
  $1/4$

19) QID: 29473

The proof of the formula for the length of a curve depends strongly on which of the following theorems?

- Mean value theorem for derivatives  
 Theorem of product rule  
 Fundamental theorem of calculus  
 Pythagorean theorem

20) QID: 29668

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Compute the length of the smooth arc  
 $y = \ln |\cos x|$  on  $[0, \pi/4]$ .

- $\ln(\sqrt{2} + 1) - e$
- The arc length is not finite.
- $\ln(\sqrt{2})$
- $\ln(\sqrt{2} + 1)$

21) QID: 11948

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Find the vertical asymptotes  
of the curve:

$$y = \frac{x^2 - x - 6}{x^2 + x - 2}$$

- $x = -2, x = 1, \text{ and } x = 3$
- $x = -2 \text{ and } x = 1$
- $x = 1$
- There are no vertical asymptotes.